# 2018 Rocky Mountain Regional Programming Contest 

## Solution Sketches

## Credits

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## A - Quality-Adjusted Life-Year (63/72)

- Simple, do what is asked of you.


## D - H-Index (36/246)

- Find the maximum $h$ such that there are at least $h$ values that are at least $h$.
- Sort the array (largest to smallest)
- For each $h$ (from 0 to $n$ ), the largest $h$ numbers are at the beginning of the array, so just check if the $h$-th value is at least $h$.


## G - Neighborhood Watch (36/141)

- How many intervals contain a "special" house?
- Count the number of bad paths and subtract from total number of intervals.
- Look at the size of the gaps between special houses.
- If the gap has $g$ houses, then the number of bad paths in that gap is $g(g+1) / 2$.


## H - Small Schedule (35/114)

- Bin packing with two sizes
- Fill with large ones, then with 1's
- Be careful of off-by-one errors


## C - Forest for the Trees $(14 / 86)$

- Which trees can obstruct the view?
- $\left(k * x_{b} / g, k * y_{b} / g\right)$ where $g=\operatorname{gcd}\left(x_{b}, y_{b}\right)$ is the next tree in the way.
- Look at the values of $k$ such that the corresponding trees are in the rectangle.
- Can be done in constant time by looking at linear inequalities.


## E - Driving Lanes (5/9)

- Dynamic programming
- Define $f(n, L)=$ the shortest distance to drive the first $n$ straightaways and be in lane $L$.
- For each state, try changing to each of the other lanes (if possible).


## I - Mr. Plow King (5/14)

- How to maximize the minimum spanning tree?
- Kruskal's algorithm tells us that we should greedily take the shortest edge if it doesn't create a cycle.
- You must include edges 1 and 2. The only way to not include edge 3 is to make a triangle (with 1, 2, 3).
- Then you must include edge 4. To not use edge 5 and 6 , connect those edges into your connected component.
- Then you must include edge 7. Etc.
- At some point, you can use all remaining edges in the MST. Put them in a path.
- In general:
- Make a giant connected component with lots of small edges.
- Make a long path of large edges.


## J - Rainbow Road Race (3/3)

- Travel through edges to get colors. Return to the start location with all colors with the shortest travel time.
- Create a new graph where the nodes are the pair: (location, set of colors you have).
- For each edge (from location $i$ to $j$ ) create an edge from $(i, S)$ to $(j, S \cup\{$ color of edge $\})$ for all possible color sets $S$.
- Run a shortest path algorithm from $(1,\{ \})$ to (1, $\{R, O, Y, G, B, I, V\})$.


## B - Gwen's Gift (2/10)

- There are $(n-1)$ ! valid sequences, for each first element there are $(n-2)$ ! valid sequences and so on
- Keep track of the sums modulo $n$.
- For each position, go from 1 to $n-1$ skipping the invalid elements until you get to the desired index
- An element is invalid if (a) the prefix sum is 0 or (b) we have already seen the prefix sum (both $\bmod n)$
- $20!>10^{18}$ - we care only about the last 20 elements, the rest are all 1's


## B - Gwen's Gift (2/10) (...continued...)

- Another way to think about the problem: the partial sums of the array (modulo $n$ ) are non-zero and distinct.
- So the partial sums modulo $N$ form a permutation of $1,2, \ldots, n-1$.
- Generate the $k$ th permutation (but order based on the original sequence).


## F - Treasure Spotting (0/23)

- Relatively simple geometry, most cases covered in samples
- Line segment intersection
- Use integer arithmetic (do not use floating point)

